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Pre Ph. D. Course work Examination 2019-20

MATHEMATICS

PAPER II: CW – 02 (TOOLS AND TECHNIQUES)

Model question paper

[Set – V]

Duration - 3.00 Hrs

Max. Marks - 80

Note: Section - A is Compulsory. Answer one question from each unit of Section - 'B' carrying equal marks

Section - A

1. Answer the following questions in brief.

2 X 10 = 20

- (I) How can we write the following in LaTeX? - (a) \in Symbol (b) Binomial coefficient
- (II) Write LaTeX structure for - (a) Limit (b) Integration
- (III) What is the meaning of following commands in LaTeX? - (a) \neg (b) \cup
- (IV) Define equilibrium of a fuzzy complement c.
- (V) Define Dual triple.
- (VI) State first characterization theorem of fuzzy complement.
- (VII) Is there a function which does not satisfy the Banach contraction principle but has a fixed point?
- (VIII) Define fixed point theorem for multi-function with an example.
- (IX) What does Fejer-Lebesgue theorem state?
- (X) What is integral modulus of continuity?

Section - B

12 X 5 = 60

UNIT - I

- 2. Describe document classes and document sectioning in LaTeX.**
- 3. Discuss about creating documents in LaTeX.**

UNIT - II

- 4. Let $f: X \rightarrow Y$ be an arbitrary crisp function. Then for any $A \in \mathcal{F}(X)$, Show that $\alpha_{[f(A)]} \supseteq (f \circ \alpha_A)$, but conversely.**

- 5. Let the membership grade function of fuzzy sets A, B and C be defined as**

$$A(x) = \frac{x}{x+2}, B(x) = 2^x, C(x) = \frac{1}{[1+10(x-2)^2]}$$

On the universal set $X = \{0, 1, 2, 3, \dots\}$ and $\mu_{f(A)}(x) = 2^x$ for all $x \in X$. Then use the extension principle to derive $f(A)$, $f(B)$ and $f(C)$.

UNIT - III

- 6. State and prove Banach fixed point theorem.**
- 7. State and prove Schauder fixed point theorem.**

UNIT-IV

- 8. Describe the following.**
 - (a) (E, \sum)
 - (b) (C, \sum)
 - (c) (N, \sum)
 - (d) Abel sum.
- 9. State and prove necessary and sufficient condition for the regularity of the (N, \sum) method.**

UNIT - V

- 10. What is summability of series? Describe summability Fourier series.**
- 11. Describe the following**
 - (a) Delta value Poussen's test
 - (b) Integration of Fourier series.