

# ATAL BIHARI VAJPAYEE VISHWAVIDYALAYA BILASPUR (C.G.)

Pre Ph. D. Course work Examination 2019-20

## MATHEMATICS

PAPER II: CW – 02 (TOOLS AND TECHNIQUES)

### Model question paper

### [Set – V]

Duration - 3.00 Hrs

Max. Marks - 80

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*Note: Section - A is Compulsory. Answer one question from each unit of Section - 'B' carrying equal marks*

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#### Section - A

##### 1. Answer the following questions in brief.

**2 X 10 = 20**

- ((I) How can we write the following in LaTex? - (a)  $\in$  Symbole (b) Binomial coefficient
- ((II) Write LaTex structure for - (a) Limit (b) Integration
- ((III) What is the meaning of following commands in LaTex? - (a)  $\backslash$ neg (b)  $\backslash$ cup
- ((IV) Define equilibrium of a fuzzy complement c.
- ((V) Define Dual triple.
- ((VI) State first characterization theorem of fuzzy complement.
- ((VII) Is there a function which does not satisfy the Banach contraction principle but has a fixed point?
- ((VIII) Define fixed point theorem for multi-function with an example.
- ((IX) What does Fejer-Lebesgue theorem state?
- ((X) What is integral modulus of continuity?

#### Section - B

**12 X 5 = 60**

#### UNIT - I

##### 2. Describe document classes and document sectioning in LaTex .

##### 3. Discuss about creating documents in LaTex.

#### UNIT - II

##### 4. Let $f: X \rightarrow Y$ be an arbitrary crisp function. Then for any $A \in \mathcal{F}(x)$ , Show that $\alpha_{[f(A)]} \supseteq (f\alpha_A)$ , but conversaly.

##### 5. Let the membership grade function of fuzzy sets A, B and C be defined as

$$A(x) = \frac{x}{x+2}, B(x) = 2^x, C(x) = \frac{1}{[1+10(x-2)^2]}$$

On the universal set  $X = \{0, 1, 2, 3, \dots\}$  and If  $f(x) = 2^x$  for all  $x \in X$ .  
Then use the extension principle to derive  $f(A)$ ,  $f(B)$  and  $f(C)$ .

#### UNIT - III

##### 6. State and prove Banach fixed point theorem.

##### 7. State and prove Schauder fixed point theorem.

#### UNIT-IV

##### 8. Describe the following.

- (a) (E, 1sum) (b) (C, 2sum) (c) (N, p sum) (d) Abel sum.

##### 9. State and prove necessary and sufficient condition for the regularity of the (N, p) method.

#### UNIT - V

##### 10. What is summability of series? Describe summability Fourier series.

##### 11. Describe the following

- (a) Delta value Poussen's test (b) Integration of Fourier series.