

# ATAL BIHARI VAJPAYEE VISHWAVIDYALAYA BILASPUR (C.G.)

Pre Ph. D. Course work Examination 2019-20

## MATHEMATICS

PAPER II: CW – 02 (TOOLS AND TECHNIQUES)

### Model question paper

### [Set – II]

Duration - 3.00 Hrs

Max. Marks - 80

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*Note: Section - A is Compulsory. Answer one question from each unit of Section - 'B' carrying equal marks*

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#### Section - A

##### 1. Answer the following questions in brief.

**2 X 10 = 20**

- (i) What is Latex?
- (ii) Write Latex structure for Binomial coefficient.
- (iii) If  $A = \frac{1}{x} + \frac{4}{y} + \frac{1}{z}$ , find extended compliment of A.
- (iv) Prove that the standard fuzzy complement is not cut worthy property.
- (v) Define Lipschitz continuous function?
- (vi) Write an example of Lipschitz continuous function which is not differentiable?
- (vii) What is regularity of a Summation method?
- (viii) What is linear Transformation T of the sequence?
- (ix) What is order of approximation?
- (x) When a function is said to satisfy Lipschitz condition of order?

#### Section - B

**12 X 5 = 60**

#### UNIT – I

##### 2. Discuss about Latex workflow?

##### 3. Discuss the difference between Latex and MikTex.

#### UNIT – II

##### 4. Prove first decomposition theorem for A where $X = \{x_1, x_2, x_3, x_4, x_5\}$ and $A = .2/x_1 + .4/x_2 + .6/x_3 + .8/x_4 + 1/x_5$

##### 5. Let A and B be fuzzy sets defined on the universal set $X = Z$ , where membership functions are given by

$$A(x) = 5/(-1) + 1/0 + .5/1 + .3/2 \quad \text{And} \quad B(x) = .5/2 + 1/3 + .5/4 + .3/5.$$

Let a function  $f : X \times X \rightarrow X$  be defined for all  $x_1, x_2 \in X$  by  $f(x_1, x_2) = x_1 + x_2$  calculate  $f(A, B)$ .

#### UNIT – III

##### 6. State and prove Brower's fixed point theorem.

##### 7. Let X be a uniformly convex Banach space and $C \subset X$ be non – void closed bounded And convex. If $f : C \rightarrow C$ is a no – expansive then f has a fixed point in C.

#### UNIT – IV

##### 8. Show that Eular method is regular.

##### 9. Write short notes on following

- (i) (E,1) Sum (ii) (N, P<sub>n</sub>) Sum (iii) (H, K) Sum (iv) (C, K) Sum

#### UNIT – V

##### 10. State and prove Fejer's theorem.

##### 11. Derive Dirichlet's Integral and obtain necessary and sufficient condition that the series $a_0/2 + (\sum_{n=1}^{\infty} h a_n \cos nx + b_n \sin nx)$ converges to a sum s.

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