

**PD-256**  
**M.A./M.Sc. Mathematics (SECOND SEMESTER)**  
**Examination- JUNE-2021**  
**Compulsory/Optional**  
**Group -**  
**Paper-IV**  
**COMPLEX ANALYSIS (II)**

**Time:- Three Hours ]**

**[Maximum Marks:80**

**नोट :** दोनों खण्डों से निर्देशानुसार उत्तर दीजिए। प्रश्नों के अंक उनके दाहिनी ओर अंकित हैं।

**Note:** Answer from Both the Section as Directed. The Figures in the right-hand margin indicated marks.

**Section-A**

**1. Answer the following question: 1x10**

- a. Wallis formula is-----
- b. What is the Riemann zeta function?
- c. Define function element of  $z$ .
- d. What is Natural boundary?
- e. Define Harmonic conjugate.
- f. What is poisson kernel?
- g. Define convex function.
- h. Write standard form for an entire function.
- i. Define Bloch's constant.
- j. Write univalent function.

**2. Answer the following question: 2x5**

- (a) If  $|z| \leq 1$  and  $P \geq 0$ . Then  $|1-E_p(z)| \leq |z|^{P+1}$  when  $E_p(z)$  is elementary factor.
- (b) Find the radians of convergence for  $\sum_{n=1}^{\infty} \left( \frac{z^n}{2^{n+1}} \right)$
- (c) Write Dirichlet Region.
- (d) Find the order of the function  $\cos Z$  and  $\sin Z$
- (e) Write the statement of  $\frac{1}{4}$  - Theorem.

**Section-B**

**Answer any five the following question: 5x12**

- 3. State & prove Legendre's duplication formula.
- 4. State & prove Euler's product formula.
- 5. State & prove schwarz's reflection principle for symmetric region.
- 6. state & prove monodromy theorem.
- 7. state & prove Harnack's Inequality.
- 8. Let  $G$  and  $\Omega$  be regions such that there is a one-one analytic function of  $G$  an to  $\Omega$ . Let  $a \in G$  and  $\varphi = F(a)$ . If  $g_a$  and  $V\varphi$  are the greens fuctions for  $G$  and  $\Omega$  with singularities  $a$  and  $\varphi$  respectively, then  $G_a(z) = V\varphi(f(z))$
- 9. state & prove Jense's formula.
- 10. state & prove Hadamards three circles theorem.
- 11. state & prove Blochs theoem.
- 12. state & prove Schottkys theorem.